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Abstract—Resource management (RM) is a critical action in systems with limited resources such as sensor networks. Efficient RM depends heavily upon the availability of accurate information on the state of available resources. However, exchange of state information incurs an overhead on the system. In this paper, the sensing and computing resource management in sensor networks is considered. A lossless, distributed source-coding framework is presented to model the exchange of state information. The framework enables the characterization of the interplay between the performance and overhead of RM by leveraging the correlation among the state information of various nodes. Moreover, the proposed framework enables an improved estimate of the lower bound for the minimum control overhead necessary to accurately describe the state of nodes in the network. This improvement is achieved by exploiting the correlation among the state information of nodes as well as available information on prior resource allocation actions as side information.

Index Terms—Sensor networks, resource management, distributed computing, control overhead, information theory, distributed source coding, side information.

I. INTRODUCTION

Resource management (RM) is a critical action in systems with limited resources such as sensor networks. In this paper, we focus on the computing and sensing resource-management problem in sensor networks. Managing sensing and computing resources is important in many sensor-network applications such as pervasive computing, mobile computing, battlefield surveillance, control and situational awareness, and target tracking [1]–[3]. In such applications, local agents (users and sensor nodes) in the field as well as remote users submit sensing and computing requests to the system. Sensor networks respond to these requests by means of collaborative processing while using distributed sensing and computing resources. In this paper, resource allocation refers to assigning tasks associated with requests to sensor nodes. Hence, we use the term task assignment (TA) and resource allocation interchangeably in this paper. Furthermore, the proposed analytical framework in this paper can be applied to any arbitrary resource management problem in distributed systems such as dynamic wavelength assignment in optical networks and computing resource management in cloud systems.

Efficient RM depends heavily upon the availability of accurate resource-utilization information, which we term state information [3]–[6]. However, the inevitable exchange of state information consumes valuable energy and communication resources and incurs a cost in the system termed RM control overhead. Recently, information theory has been used to characterize the control overhead of networks [7]–[10], where the control overhead is thought of as the rate of information exchange. In such works, point-to-point rate-distortion theory [11] has been utilized to capture the trade-off between control overhead and the distortion in the state information (consequently the performance of a given protocol).

Different from the rate-distortion approach, here we present a lossless, distributed source-coding framework to characterize the interplay between RM performance and the overhead it incurs in sensor networks. This has been done by taking into account the correlation among the state information of various nodes while observing that an RM protocol can affect the correlation among the state information of nodes. Notably, our framework ties each RM protocol to an overhead. This is because in a lossless distributed source-coding framework, the correlation among the state information specifies the rate region for accurate communication, determined by constraints on the rate of each node and sum of the rate of nodes. We also derive an improved lower bound for the rate region (associated with an arbitrary RM protocol) by exploiting the correlation among the state information of nodes as well as knowledge of prior resource-allocation actions as side information.

We emphasize that the interplay addressed by rate-distortion–based formulations is different from that addressed by our framework. Rate-distortion–based formulations characterize the trade-off between the rate of information and distortion by considering a class of codes that satisfies the rate and distortion constraints. On the other hand, our framework characterizes the interplay between performance of RM and its overhead by means of a class of protocols, which each satisfies certain performance and overhead while assuming sensor-network applications for which distortion in the state information is not tolerable. For example, a constraint on the control overhead will yield a class of admissible RM-protocols, from which we can extract the best achievable RM performance.

This paper is organized as follows. A brief overview of related work is presented in Section II. Section III defines the sensor network and resource management model. In Section IV, a distributed source-coding framework for exchanging the
state information of nodes is formulated and its rate region is characterized. Numerical results for an example sensor network and discussion on the interplay between the control overhead and RM performance are presented in Section V. Finally, concluding remarks are presented in Section VI.

II. RELATED WORK

Recently, information theory has been adopted for characterizing the control overhead of networks. The pioneering work presented by Gallager [12] is one of the earliest contributions that used information theory in characterizing the network overhead for tracking source and receiver addresses. In [7] and [8] the minimum overhead of maintaining state information (link state and motion state, respectively) to be used in routing protocols across a mobile ad hoc network is formulated as a rate-distortion problem. The assumption in [7] and [8] is that the state information associated with various nodes/links are mutually independent; hence, the rate-distortion formulation is considered for a single component. The authors of [10] use rate-distortion theory to investigate the optimal timing for updating the bandwidth information of the links. In [9], the relation between network performance and information rate is captured by extending the definition of distortion measure to capture network performance.

It is to be noted that all the aforementioned works consider point-to-point information theory in characterizing the interplay between network overhead and distortion. Network information theory [11], on the other hand, provides strong tools for characterizing the information exchange in a distributed fashion when there is correlation among the state information of different sources. However, to the best of our knowledge networked information theory has not been used heretofore in investigating the control overhead of networks. While distributed source coding theory has been widely used in sensor networks in the last decade, its utility has been limited to the context of distributed sensing [13]. Although tracking the state of nodes in a network can be viewed as a distributed-sensing problem, the signal of interest here is tied to the network characteristics, protocols and policies, which can collectively define the performance of the network. Here, the distributed source coding model may warrant extension or modifications to capture the information characteristics and their availability in various part of the network. In this paper we use the generality of distributed source coding theory to characterize the interplay between performance and the control overhead of RM in sensor networks through the correlation among state information of various nodes.

III. SYSTEM MODEL

In this section, we model sensor networks and resource management. The notation and terminology used in this paper are summarized in Table I. Consider a sensor network consisting of clusters of sensors as shown in Fig. 1. Each cluster has a control node (CN) that is responsible for monitoring the resource utilization, maintaining the state information of nodes and performing resource allocation. Here, the problem of investigating the control overhead of sensor networks is broken down to the same problem for individual clusters of nodes. Hence, we will focus on one cluster hereafter with the understanding that the same procedure will be applied to all clusters of the network.

### A. Resource allocation and information exchange

The main role of sensor nodes in a cluster is to process tasks and send the state (resource utilization) information to the CN. We assume that the state information of nodes may be used by RM or other network protocols. We use the queue size of tasks (awaiting tasks) in a node to estimate the resource availability at the node. We term the intervals \([t_{U_{i-1}}, t_{U_i}], [t_{S_{i-1}}, t_{S_i}],\) and \([t_{A_{i-1}}, t_{A_i}]\) as update interval, sampling interval, and TA interval, respectively, as shown in Fig. 2. We assume that each

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<th>Table I: Table of Notations</th>
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<tr>
<td>Symbol</td>
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<tr>
<td>(N)</td>
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<tr>
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<td>(t_U)</td>
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<td>(t_S)</td>
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<tr>
<td>(Z(F_{TA}))</td>
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![Fig. 1. A sensor system and its clusters.](image-url)
update interval consists of $n$ sampling and TA intervals. Note that for convenience we assume equal number of sampling and TA instances in an update interval; however, these instances are not assumed to be synchronized.

A sensor node $i$ encodes and then sends $n$ samples of its queue size $Q_i(t)$, sampled at the instants $t_{S_j}$, to the CN at the end of each update interval. We assume that the CN and its constituent nodes in a cluster communicate directly over noiseless links. We further assume that sensing and computing requests arrive at the CN at random times while each request is comprised a random number of tasks. The CN buffers tasks upon arrival and assigns them (total $M_j$ tasks) to the nodes at $t_{A_j}$ based upon a prescribed (static) RM protocol. We represent the way that CN assigns tasks to sensor nodes by a function $F_{TA}$, which may follow different objectives such as load balancing and minimizing energy consumption of the network. More specifically, we write $F_{TA}(M_j) = \mathbf{Y}(t_{A_j})$, where $\mathbf{Y}(t_{A_j}) = (Y_{1t_{A_j}}, Y_{2t_{A_j}}, \ldots, Y_{Nt_{A_j}})$ with the constraint $\sum_{i=1}^{N} Y_{it_{A_j}} = M_j$. Refer to Table I for the definition of notations. Here, the $Y_{ij}$s are independent and identically distributed (i.i.d) across time (i.e., for $j = 1, \ldots, n$).

**B. Dynamics of queue sizes**

The dynamics of the queue size of a node is governed by the random variables associated with the number of tasks being processed at the node, tasks being generated in the internal system of the node (by the node’s operating system or software agents), tasks being received from local agents, and tasks being assigned to the node by the CN. Note that samples of queue sizes, $Q_i(t)$, at instants $t_{S_j}$ for $j = 1, \ldots, n$ are correlated due to the dependency of the queue size at any sampling time on the number of tasks queued at the node at previous sampling times. However, jumps in the queue size are independent in time because all the random variables affecting the queue size can be assumed to be independent in time (i.e., instants $t_{S_j}$ for $j = 1, \ldots, n$). More precisely, we represent the dynamics of the queue size by jumps in the queue size as

$$X_i = Y_i + U_i + L_i - P_i,$$

(1)

**C. Correlation among random variables**

As depicted for a generic random variable in Fig. 3, the random variables affecting the queue size of a node according to (1) are independent in time but they may be correlated across sensor nodes (except for $U_i$ and $P_i$, which are independent across nodes because they are node specific). Generally, the $Y_i$s of different nodes can be correlated due to the adoption of certain $F_{TA}$ by the CN. We will consider the following examples of $F_{TA}$, which will illustrate the correlation among the $Y_i$s of different nodes due to the system adopting a resource-allocation protocol, $F_{TA}$, say. First consider the protocol $F_{TA}$, that randomly distributes tasks among sensor nodes based upon a uniform probability mass function. Clearly, it is expected in this case that the $Y_i$s exhibit minimum correlation; note however that correlation may still exist due to the constraint $\sum_{i=1}^{N} Y_{ij} = M_j$. In the second example, $F_{TA}$, evenly distributes tasks among nodes, which results in a high degree of correlation among the $Y_i$s. Other in-between scenarios can be associated with the $F_{TA}$s that exploit the characteristics of the nodes and the state information in implementing resource allocation.

Similarly, the $L_i$s, for $i = 1, \ldots, N$, may be correlated due to task assignment protocol of local agents in the cluster (the way local agents directly assign tasks to the nodes). As the first example of task assignment protocol, let us assume that agents assign tasks to their closest node as depicted in cluster 2 of the network shown in Fig. 1. In this scenario, we assume nodes and agents are not mobile; as such, we can assume that each agent is associated to a specific sensor node (e.g., the closest) and will only submit tasks to that node. In this case, the correlation among $L_i$s is minimum because of the random and independent task assignment of agents. In the next example, we assume that agents evenly distribute their tasks among all the nodes in the cluster as has been shown in cluster 1 in Fig. 1. In this case, there is a higher degree of correlation among the $L_i$s than that in the previous example. Once again, in-between scenarios can exist for example when users assign tasks to their closest node while they are mobile and the closest node change in time.

Now based upon the correlation among the random variables affecting the queue size of a node, we can conclude that $X_i$s of different nodes (for $i = 1, \ldots, N$) can also be correlated. We represent the correlation among $X_i$s by $C(F_{TA})$, which as discussed earlier, depends upon $F_{TA}$, the task-assignment protocol of agents and the RM policy.

**IV. INFORMATION-THEORETIC FRAMEWORK**

**A. Distributed Source Coding Model**

Assume that at each update instant node $i$ uses its encoder to encode $X_i^n = (X_{i1}, X_{i2}, \ldots, X_{in})$ separately from other nodes and then sends it to the CN. We term the information about the prior resource-allocation actions, $Y_i$s, as side
information. We assume the statistical characteristics of \( X_i \) and \( Y_i \) are available, as discussed in Section III. The CN uses its decoder to decode and reconstruct the state of nodes using the correlation among \( X_i \)'s and the side information \( Y_i \)'s. Specifically, the reconstructed state of node \( i \) is denoted by \( X_i^R = (\bar{X}_{i1}, \bar{X}_{i2}, \ldots , \bar{X}_{in}) \) and the probability of error is \( P_e^{(n)} \triangleq P\{(X_i^R, X_i^N) \neq (X_i^N, X_i^N)\} \). Figure 4 illustrates this formulation schematically for a cluster with \( N \) nodes. Our formulation is an extension of Slepian-Wolf Theorem [14] to distributed lossless source coding with multiple side information.

An \( N \)-tuple \( (R_1, \ldots , R_N) \) is said to be achievable for distributed lossless source coding if there exists a sequence of codes with these rates such that \( \lim_{n \to \infty} P_e^{(n)} = 0 \). Note that the control overhead of a specific RM protocol is defined as

\[
W(F_{TA}) \triangleq \sum_i R_i. \tag{2}
\]

In our framework, protocol \( F_{TA} \) leads to certain level of correlation among the state information, \( C(F_{TA}) \), which subsequently specifies the overhead \( W(F_{TA}) \) based upon the distributed source coding model. Therefore, the performance \( Z(F_{TA}) \) and overhead \( W(F_{TA}) \) are tied together through \( C(F_{TA}) \), which enables the characterization of the interplay between performance and overhead of the RM.

Fig. 4. The proposed distributed source coding model with side information to characterize the control overhead. For the ease of reference and discussion of the theory, we define:

**Formulation 1.** A distributed source coding problem that does not use \( Y_i \)'s and nor does it use the correlation among \( X_i \)'s. This formulation is equivalent to \( N \) separate Shannon’s lossless source coding problems.

**Formulation 2.** A distributed source coding problem that uses \( Y_i \)'s but it does not use the correlation among \( X_i \)'s. This formulation is equivalent to \( N \) conditional lossless source coding problems (single source coding problem with side information at the encoder and the decoder [11]).

**Formulation 3.** A distributed source coding problem that uses the correlation among \( X_i \)'s but it does not use \( Y_i \)'s. This formulation is a Slepian-Wolf problem.

**Formulation 4.** A distributed source coding problem that uses both \( Y_i \)'s and the correlation among \( X_i \)'s. This is our formulation in this paper.

Note that Formulations 1 and 2 fall in the area of point-to-point information theory.

B. Characterizing the rate region

We begin the characterization of the rate region of Formulation 4 by considering the distributed source coding model for a cluster with two nodes. The achievable rate region of the formulations mentioned in the last section has been depicted in Fig. 5. Note that in Fig. 5, we have shown the rate region of Formulations 2 and 3 in the special case when \( H(X_1|X_2) < H(X_1|Y_1) \) and \( H(X_2|X_1) < H(X_2|Y_2) \), where \( H(\cdot|\cdot) \) represents the conditional entropy. Characterization of the achievable rate region of Formulation 3 has been presented by Slepian and Wolf in [14]. The achievable rate region of Formulation 2 is also known [11]. Characterizing the achievable rate region of the Formulation 4 is straightforward and can be explained as follows. Consider a special case in which there is only one encoder that jointly encodes the state information of the two nodes while the CN decodes the code for both source using side information. In this case the outer bound of the sum-rate, defined as \( R_1 + R_2 \), for Formulation 4 can be written as \( R_1 + R_2 \geq H(X_1, X_2|Y_1, Y_2) \). In general, however, this bound may not be achievable since nodes are encoding the sources separately (this is why it is termed outer bound). Now consider the case when nodes encode the sources separately while each node having access to the other node’s state information. In this case, the rate of a node should satisfy \( R_1 \geq H(X_1|X_2, Y_1, Y_2) \) based on Formulation 2. Combining these bounds results in the outer bound for the optimal rate region of Formulation 4, which can easily be shown to be achievable and tight (with a proof similar to that of the Slepian-Wolf Theorem [15]) and therefore improves the lower bound on the minimum information rates.

**Theorem 1.** The optimal rate region for the problem in Formulation 4 with two nodes is

\[
R_1 \geq H(X_1|X_2, Y_1, Y_2),
\]

\[
R_2 \geq H(X_2|X_1, Y_1, Y_2)
\]

and

\[
R_1 + R_2 \geq H(X_1, X_2|Y_1, Y_2).
\]

Theorem 1 can be extended to an arbitrary number of nodes in the cluster as follows.

**Theorem 2.** Let \( S \subset \{1, 2, \ldots , N\} \). The optimal rate region for the problem in Formulation 4 with \( N \) nodes is

\[
\sum_{j \in S} R_j \geq H(X(S)|X(S^c), Y(S \cup S^c)),
\]

where \( X(S) \) is the set of \( X_i \)'s for \( i \in S \) and \( X(S^c) \) and
$Y(S \cup S^c)$ are defined likewise. Note that in this special case of distributed source coding problem the rate region of the framework depicted in Fig. 4 would be the same as the one stated by Theorem 1 and 2 even if the side information $Y_i$s were only available at the decoder. However, in lossy distributed source-coding problems these two cases would result in different rate regions. The next point to note here is that the lower bounds derived based on these approaches, are asymptotically achievable (as the number of samples in an update interval goes to infinity, i.e., $n \to \infty$); hence, they provide bounds on the overhead of the network [7]-[10].

V. Numerical Evaluation

Theorems 1 and 2 provide analytical expressions of the lower bound for the minimum state information rate of nodes in a cluster. In this section, we consider a specific example of a sensor network and provide the numerical results calculated for the minimum control overhead of RM. For simplicity, we consider a cluster with two nodes.

\begin{align*}
C(F_\mathcal{PA}) \text{ through } \Delta Y, \text{ which represents the number of excess tasks assigned to node 1 compared to node 2. In a similar way, the correlation between } L_i \text{s can be modeled by } L_1 = L_2 + \Delta L. \text{ Here, } \Delta L \text{ depends on the task assignment protocol of local agents. Note that the correlation among } L_i \text{s also affect the correlation among } X_i \text{s. Therefore, } F_\mathcal{PA} \text{ and task assignment protocol of local agents affect } C(F_\mathcal{PA}) \text{ through } Y_i \text{s and } L_i \text{s. In our example, we assume independent Poisson distributions for random variables with random-variable-specific Poisson parameters. With the above preliminaries and the dynamics of the queue size described in (1), we write } X_1 \text{ and } X_2 \text{ as}
\end{align*}

\begin{align*}
X_1 &= Y_2 + \Delta Y + U_1 + L_2 + \Delta L - P_1, \\
X_2 &= Y_2 + U_2 + L_2 - P_2.
\end{align*}

In our calculations, we have assumed $\lambda_{Y_2} = 6$, $\lambda_{L_2} = 3$, $\lambda_{U_1} = \lambda_{U_2} = 1$, $\lambda_{P_1} = \lambda_{P_2} = 4$, and $\lambda_{\Delta L} = \lambda_{\Delta Y} = 1$. Since all the random variables have Poisson distributions, we can numerically calculate the entropy, joint entropy and conditional entropy for different combination of the presented random variables. Moreover, we use the fact that sum of two independent Poisson random variables is a Poisson random variable and the difference of two independent Poisson random variables with parameters $\lambda_1$ and $\lambda_2$ has Skellam distribution, $p(k; \lambda_1, \lambda_2) = e^{-(\lambda_1+\lambda_2)}(\lambda_1/\lambda_2)^{k/2}I_k(2\sqrt{\lambda_1\lambda_2})$, where $I_k(z)$ is the modified Bessel function of the first kind. The assumption on the Poisson distribution is commonly adopted in literature [16], [17] for the random number of tasks.

B. Numerical results

According to (1), $X_i$ and $Y_i$ may be correlated and the level of correlation between them is affected by the dynamics of the network and the node through $U_i$, $P_i$, and $L_i$. In general, as the randomness in these variables increases the correlation between $X_i$ and $Y_i$ decreases and rate of state information increases. In the extreme case, for which events in the system are deterministic (e.g., deterministic task processing time) the $X_i$ values can be calculated based upon the $Y_i$ values at the CN, and therefore, there is no need to exchange the state information and the control overhead will be zero. In our example, when $U_i$, $P_i$ and $L_i$ have high level of randomness (large $\lambda$ parameter) then the correlation between $X_i$ and $Y_i$ decreases. Figure 6-a depicts the minimum state-information rate of node 1 as a function of $\lambda_{L_1}$, for Formulations 1, 2, and 4 calculated at points A, B, and D shown in Fig. 5, respectively. In our calculations, we have fixed the Poisson parameter of all the random variables in the system and only changed $\lambda_{L_1}$. From Fig. 6-a, we observe that as the dependency between $X_1$ and $Y_1$ decreases the rate of node 1 increases. The sum of the rates of nodes (total control overhead) for the formulations are calculated based on the sum-rate constraint in Theorem 1 and shown in Fig. 6-b. Figure 6-b also shows that the sum of the pair of rates shown in Fig. 6-a equals to the sum-rate constraint value calculated based on Theorem 1. This is due to the special position of the selected pair of rates (in Fig. 5).

We next investigate the effect of correlation between $X_1$ and $X_2$ on the control overhead. To see this effect in our example, we fixed the Poisson parameter of all the random variables

\begin{align*}
\text{A. Settings of the example}
\end{align*}

We indicated in Section III that the $Y_i$s of different nodes may be correlated due to $F_{\mathcal{PA}}$. To model the dependency between $Y_1$ and $Y_2$ in our example we simply use $Y_1 = Y_2 + \Delta Y$. In this model $F_{\mathcal{PA}}$ affects the correlation between $Y_1$ and $Y_2$ (and consequently the correlation between $X_1$ and $X_2$, i.e.,
and only changed $\lambda_{\Delta Y}$ and $\lambda_{\Delta L}$ (we assume $\lambda_{\Delta Y} = \lambda_{\Delta L}$). The minimum state-information rate of node 1 for Formulation 3 (calculated at point C in Fig. 5) and Formulation 4 are represented in Fig. 7-a. The minimum total control overhead for Formulation 3 and 4 are shown in Fig. 7-b. Notably Formulation 4 provides the smallest lower bound among other formulations for the minimum information rate of the nodes.

C. Interplay between performance and overhead

Recall that resource allocation protocols may affect the correlation between $X_1$ and $X_2$. In the results shown in Fig. 7, each $\lambda_{\Delta Y}$ value on $x$-axis can be interpreted as the representor of the $F_{TAS}$, which yields $Y_1 = Y_2 + \Delta Y$ with $\Delta Y$ following a Poisson distribution with parameter $\lambda_{\Delta Y}$. The same can be said for $\lambda_{\Delta L}$ and the task assignment protocols of local agents. Note that each $\lambda_{\Delta Y}$ on $x$-axis can be mapped to a $C(F_{TA})$ value. Similarly, the $y$-axis represents the control overhead of $F_{TA}$, i.e., $W(F_{TA})$. With this framework in place one can compare the lower bound on the minimum control overhead of various $F_{TAS}$ analytically. Next, if the performance of $F_{TA}$ is measured through a performance metric such as task completion time, energy utilization or life time of sensor network, then the interplay between $Z(F_{TA})$ and $W(F_{TA})$ can be characterized analytically.

To illustrate the interplay between the performance and control overhead of RM, consider the policies $F_{TA_1}$ and $F_{TA_2}$ introduced in Section III. The performance of $F_{TA_1}$ in terms of task completion time and load balancing has been shown to be more efficient than that for $F_{TA_2}$ in certain applications when the size of requests have a Poisson distribution [16], [17]. Therefore, in this scenario $Z(F_{TA_1}) > Z(F_{TA_2})$. Meanwhile, in this case $C(F_{TA_1}) < C(F_{TA_2})$ due to the small degree of correlation among the $Y_i$s resulted from $F_{TA_1}$, which, in turn, implies $W(F_{TA_1}) > W(F_{TA_2})$. This example demonstrates a trade-off between performance and the control overhead of RM, which can be captured analytically through our framework. Similar statements can be made about the task assignment protocol of local agents. For example, the control overhead in the task-assignment protocol shown in cluster 2 of the network in Fig. 1 is larger than that of cluster 1 as a result of the different degree of correlation among the $X_i$s. Hence, our framework paves the path to the characterization of the overhead-admissible RM protocols, from which we can extract the best achievable RM performance.

VI. CONCLUSIONS

Efficient resource management depends heavily upon the availability of accurate information on the state of available resources in the system. However, exchange of state information incurs an overhead on the network. In this paper, we formulated the exchange of state information in the network using a lossless, distributed source coding framework. We have shown that resource-management policies may lead to different levels of correlation among the state information of nodes. We then exploited the correlation among the state information of nodes to analytically characterize the interplay between the resource-management performance and overhead in a lossless source-coding framework. This framework provides an analytical tool to compare the performance and control overhead of various resource management policies. Moreover, we have derived an improved estimate of the lower bound for the minimum control overhead of RM by utilizing the correlation among the state information of nodes as well as the available information on prior resource-allocation actions as the side information.

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